



# **PARKLANDS INFANT AND NURSERY SCHOOL**

## **CALCULATION POLICY**

Approved by the Governing Body of Parklands Infant and Nursery School

Mrs S Evitts, Chair of Governors

This policy supports our school mission statement of: “To establish a life-long love of learning within a caring environment, in which we encourage all children to fulfil their potential through enjoyable and enriching experiences”.

It also supports our whole school ethos of developing the Parklands Person.



### **The Intent, implementation and Impact of our Mathematics Curriculum**

Traditionally, Maths has been taught by memorising key facts and procedures, which tends to lead to superficial understanding that can easily be forgotten. At Parklands, we believe that children should be able to select which mathematical approach is most effective in different scenarios.

All pupils can achieve in Mathematics! There is no such thing as a 'Maths person' that is the belief that some pupils can do Maths and others cannot. A typical Maths lesson will provide the opportunity for **all** children, regardless of their ability, to work through Fluency, Reasoning and Problem Solving activities.

## Intent

Maths is a journey and long-term goal, achieved through exploration, clarification, practice and application over time. At each stage of learning, children should be able to demonstrate a deep, conceptual understanding of the topic and be able to build on this over time.

There are 3 levels of learning:

- **Shallow learning:** surface, temporary, often lost.
- **Deep learning:** it sticks, can be recalled and used.
- **Deepest learning:** can be transferred and applied in different contexts.

The deep and deepest levels are what we are aiming for by teaching Maths using the Mastery approach. We aim for our learners to transfer basic Maths facts, skills and knowledge, including the subject specific vocabulary to their long-term memory.

## Implementation

Multiple representations for all- concrete, pictorial and abstract. Stem sentences are used in Maths lessons to help embed concepts.

Objects, pictures, words, numbers and symbols are everywhere. The Mastery approach incorporates all of these to help children explore and demonstrate Mathematical ideas, enrich their learning experience and deepen understanding. Together, these elements help cement knowledge so children truly understand what they've learnt.

All children, when introduced to a key new concept, should have the opportunity to build competency in this topic by taking this approach. Pupils are encouraged to physically represent mathematical concepts. Objects and pictures are used to demonstrate and visualise abstract ideas, alongside numbers and symbols.

**Concrete** – children have the opportunity to use concrete objects and manipulatives to help them understand and explain what they are doing.

**Pictorial** – children then build on this concrete approach by using pictorial representations, which can then be used to reason and solve problems.

**Abstract** – With the foundations firmly laid, children can move to an abstract approach using numbers and key concepts with confidence.

## **Impact**

- Quick recall of facts and procedures.
- The flexibility and fluidity to move between different contexts and representations of Mathematics.
- The ability to recognise relationships and make connections in Mathematics.

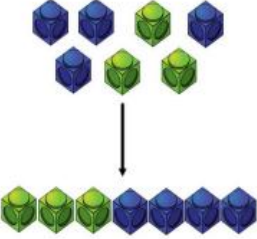
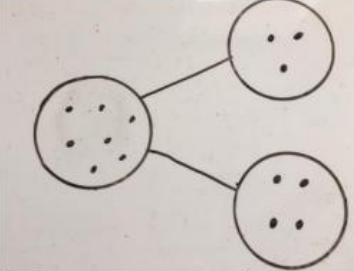
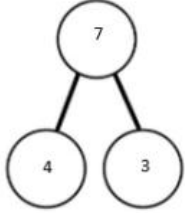
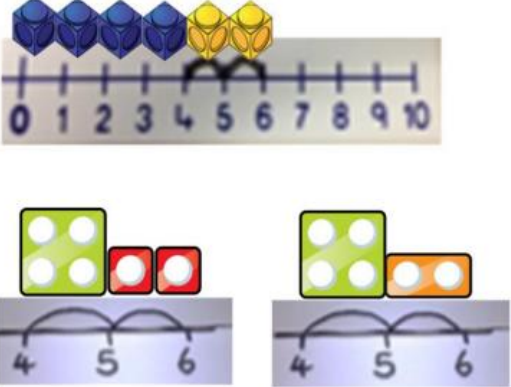
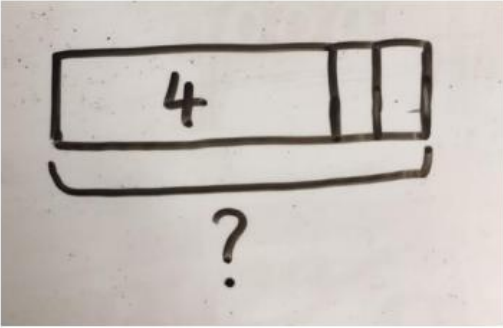

A Mathematical concept or skill has been *mastered* when a child can show it in multiple ways, using the Mathematical language to explain their ideas, and can independently apply the concept to new problems in unfamiliar situations.

In EYFS children are provided with lots of opportunities to build their knowledge and apply what they have learned using manipulatives. It is through a variety of frequent opportunities that children increase their knowledge and are able to build a mastery of mathematics.

In Key Stage 1, the following shows the progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) approach helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

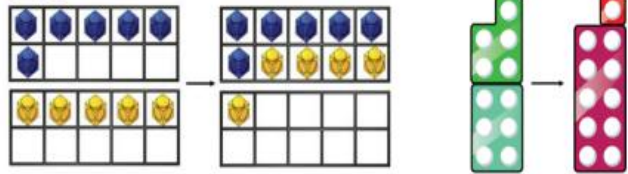
# Calculation policy: Addition

Key language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to' 'is the same as'.

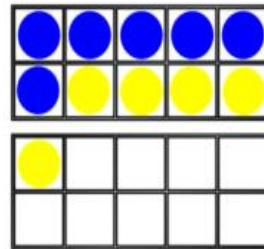
Concrete	Pictorial	Abstract
<p><b>Combining two parts to make a whole</b> (use other resources too e.g. eggs, shells, teddy bears, cars).</p> 	<p>Children to represent the cubes using dots or crosses. They could put each part on a part whole model too.</p> 	<p><math>4 + 3 = 7</math> Four is a part, 3 is a part and the whole is seven.</p> 
<p><b>Counting on using number lines</b> using cubes or Numicon.</p> 	<p>A bar model which encourages the children to count on, rather than count all.</p> 	<p>The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? <math>4 + 2</math></p> 

**Regrouping to make 10;** using ten frames and counters/cubes or using Numicon.

6 + 5



Children to draw the ten frame and counters/cubes.



Children to develop an understanding of equality e.g.

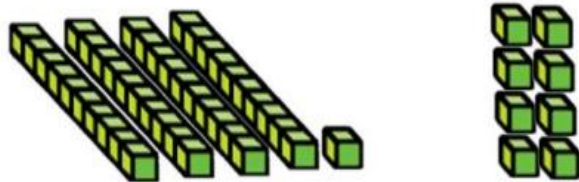
$$6 + \square = 11$$

$$6 + 5 = 5 + \square$$

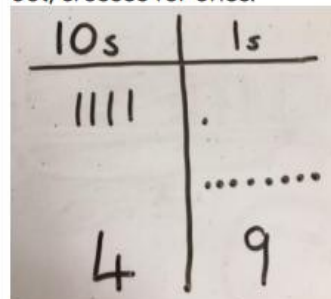
$$6 + 5 = \square + 4$$

**TO + O using base 10.** Continue to develop understanding of partitioning and place value.

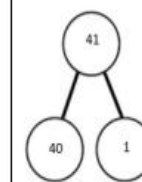
41 + 8



Children to represent the base 10 e.g. lines for tens and dot/crosses for ones.

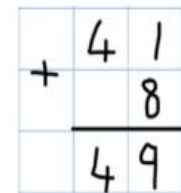


41 + 8



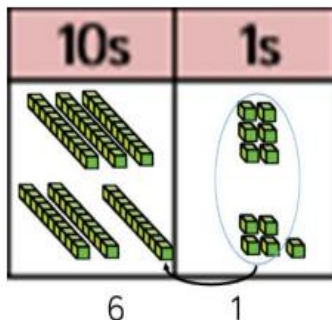
$$1 + 8 = 9$$

$$40 + 9 = 49$$

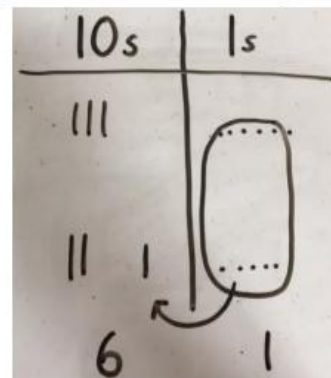


**TO + TO using base 10.** Continue to develop understanding of partitioning and place value.

36 + 25



Children to represent the base 10 in a place value chart.



Looking for ways to make 10.

36 + 25 =

1      5      36

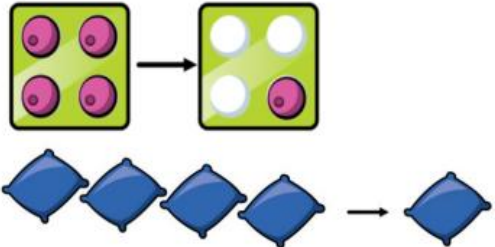
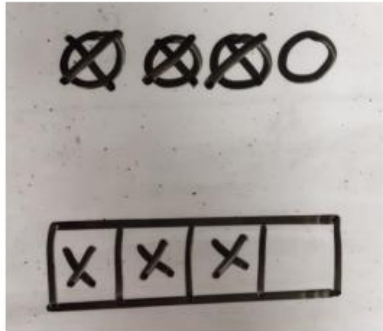

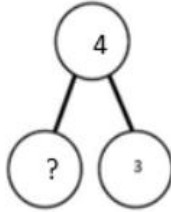
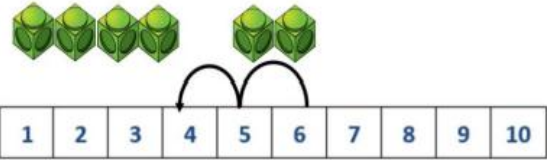
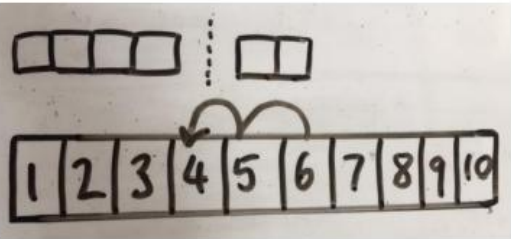

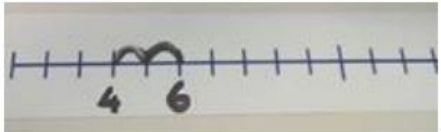
Formal method:

$$\begin{array}{r} +25 \\ 36 \\ \hline 61 \\ 1 \end{array}$$

30 + 20 = 50  
5 + 5 = 10  
50 + 10 + 1 = 61

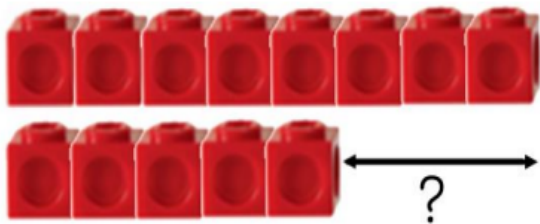
# Calculation policy: Subtraction

Key language: take away, less than, the difference, subtract, minus, fewer, decrease.

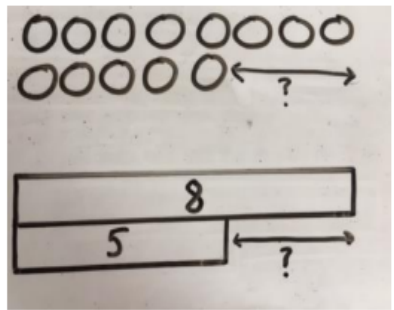
Concrete	Pictorial	Abstract				
<p><b>Physically taking away and removing objects from a whole</b> (ten frames, Numicon, cubes and other items such as beanbags could be used).</p> <p><math>4 - 3 = 1</math></p> 	<p>Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.</p> 	<p><math>4 - 3 =</math></p> <p> <math>= 4 - 3</math></p> <table border="1" data-bbox="1653 687 1935 762"> <tr> <td colspan="2">4</td> </tr> <tr> <td>3</td> <td>?</td> </tr> </table> 	4		3	?
4						
3	?					
<p><b>Counting back</b> (using number lines or number tracks) children start with 6 and count back 2.</p> <p><math>6 - 2 = 4</math></p> 	<p>Children to represent what they see pictorially e.g.</p> 	<p>Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line</p>  				

**Finding the difference** (using cubes, Numicon or Cuisenaire rods, other objects can also be used).

Calculate the difference between 8 and 5.



Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate.



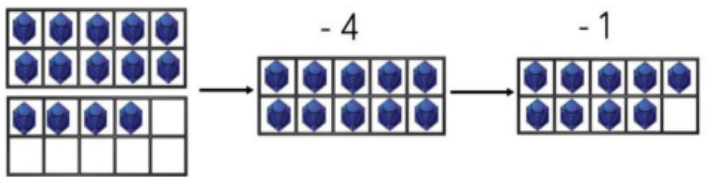
Find the difference between 8 and 5.

8 - 5, the difference is

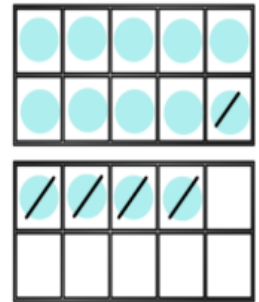
Children to explore why  
 $9 - 6 = 8 - 5 = 7 - 4$  have the same difference.

**Making 10** using ten frames.

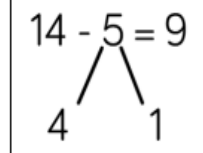
14 - 5



Children to present the ten frame pictorially and discuss what they did to make 10.



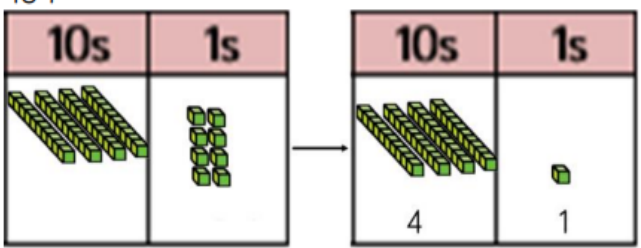
Children to show how they can make 10 by partitioning the subtrahend.



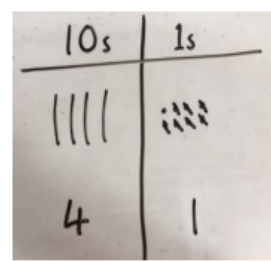
$14 - 4 = 10$   
 $10 - 1 = 9$

**Column method** using base 10.

48 - 7



Children to represent the base 10 pictorially.

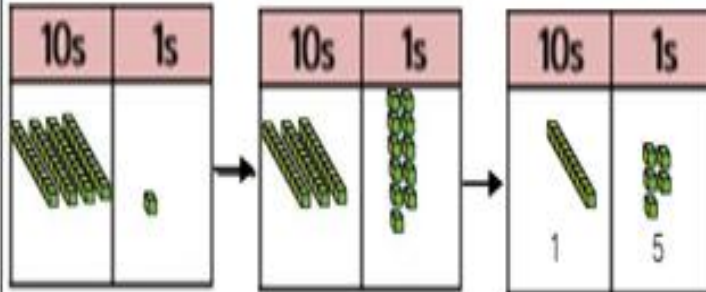


Column method or children could count back 7.

	4	8
-		7
	4	1

**Column method** using base 10 and having to exchange.

41 - 26



Represent the base 10 pictorially, remembering to show the exchange.

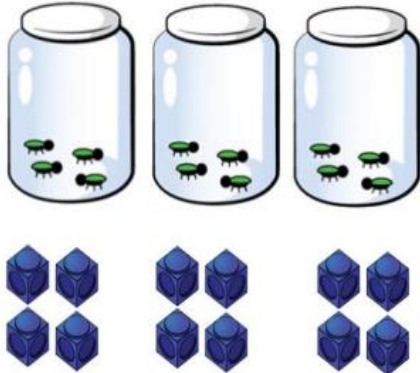
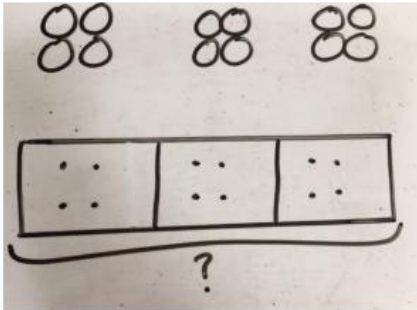
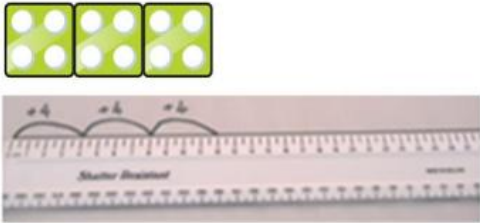
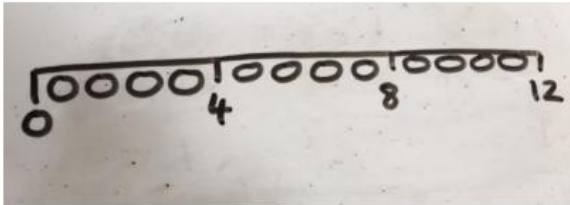
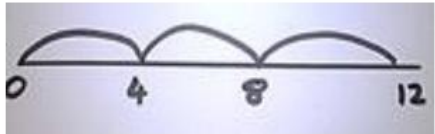


Formal column method. Children must understand that when they have exchanged the 10 they still have 41 because  $41 = 30 + 11$ .

	3	1
	<del>4</del>	1
-	2	6
	<hr/>	
	1	5

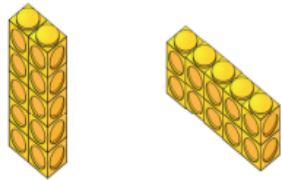
# Calculation policy: Multiplication

Key language: double, times, multiplied by, the product of, groups of, lots of, equal groups.

Concrete	Pictorial	Abstract
<p><b>Repeated grouping/repeated addition</b>  <math>3 \times 4</math>  <math>4 + 4 + 4</math>                      There are 3 equal groups, with 4 in each group.</p> 	<p>Children to represent the practical resources in a picture and use a bar model.</p> 	<p><math>3 \times 4 = 12</math>  <math>4 + 4 + 4 = 12</math></p>
<p><b>Number lines to show repeated groups-</b>  <math>3 \times 4</math></p>  <p>Cuisenaire rods can be used too.</p>	<p>Represent this pictorially alongside a number line e.g.:</p> 	<p>Abstract number line showing three jumps of four.</p> <p><math>3 \times 4 = 12</math></p> 

**Use arrays to illustrate commutativity** counters and other objects can also be used.

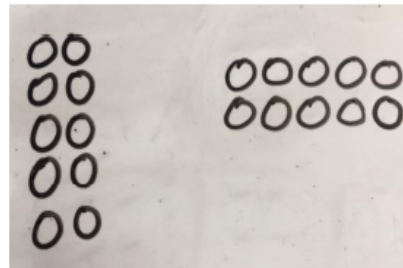
$$2 \times 5 = 5 \times 2$$



2 lots of 5

5 lots of 2

Children to represent the arrays pictorially.



Children to be able to use an array to write a range of calculations e.g.

$$10 = 2 \times 5$$

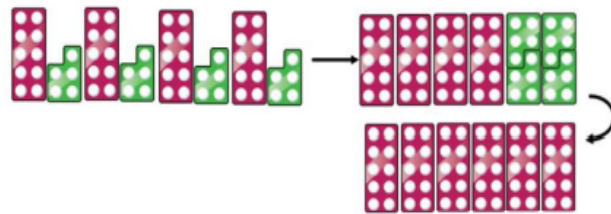
$$5 \times 2 = 10$$

$$2 + 2 + 2 + 2 + 2 = 10$$

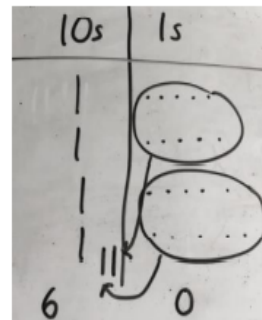
$$10 = 5 + 5$$

**Partition to multiply** using Numicon, base 10 or Cuisenaire rods.

$$4 \times 15$$



Children to represent the concrete manipulatives pictorially.



Children to be encouraged to show the steps they have taken.

$$4 \times 15$$

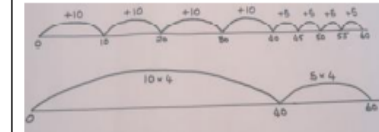
$$\begin{array}{r} 10 \\ 5 \end{array}$$

$$10 \times 4 = 40$$

$$5 \times 4 = 20$$

$$40 + 20 = 60$$

A number line can also be used



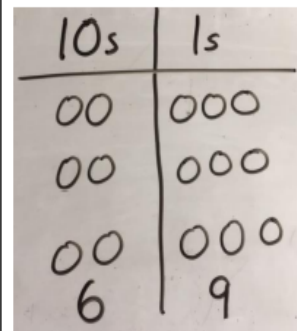
**Formal column method** with place value counters (base 10 can also be used.)  $3 \times 23$



6

9

Children to represent the counters pictorially.



Children to record what it is they are doing to show understanding.

$$3 \times 23$$

$$3 \times 20 = 60$$

$$20 \quad 3$$

$$3 \times 3 = 9$$

$$60 + 9 = 69$$

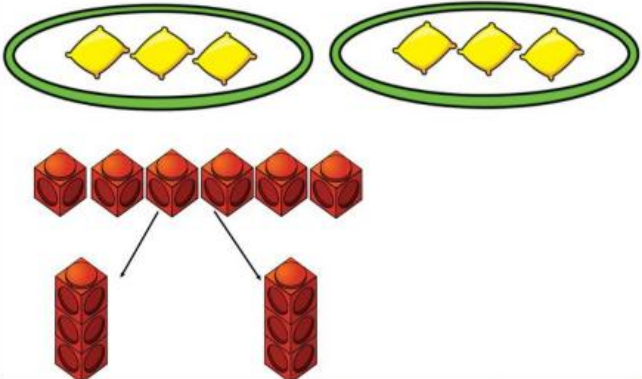
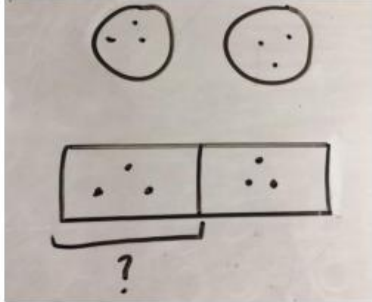
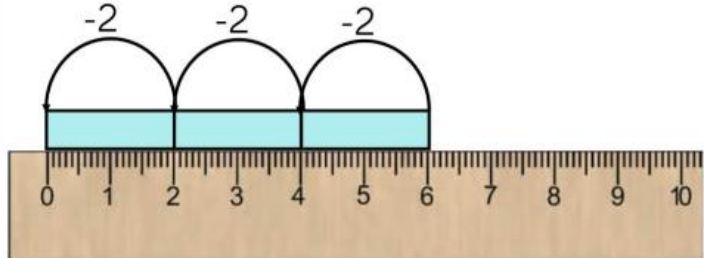
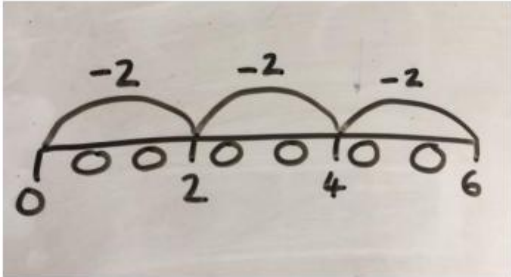
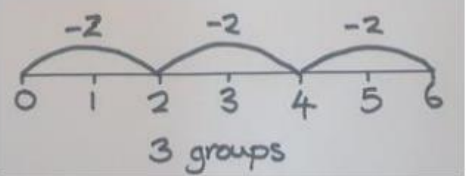
23

$\times 3$

69

# Calculation policy: Division

Key language: share, group, divide, divided by, half.

Concrete	Pictorial	Abstract		
<p><b>Sharing</b> using a range of objects.  <math>6 \div 2</math></p> 	<p>Represent the sharing pictorially.</p> 	<p><math>6 \div 2 = 3</math></p> <table border="1" data-bbox="1599 608 2018 671"> <tr> <td>3</td> <td>3</td> </tr> </table> <p>Children should also be encouraged to use their 2 times tables facts.</p>	3	3
3	3			
<p><b>Repeated subtraction</b> using Cuisenaire rods above a ruler.  <math>6 \div 2</math></p>  <p>3 groups of 2</p>	<p>Children to represent repeated subtraction pictorially.</p> 	<p>Abstract number line to represent the equal groups that have been subtracted.</p>  <p>3 groups</p>		

**2d + 1d with remainders** using lollipop sticks. Cuisenaire rods, above a ruler can also be used.

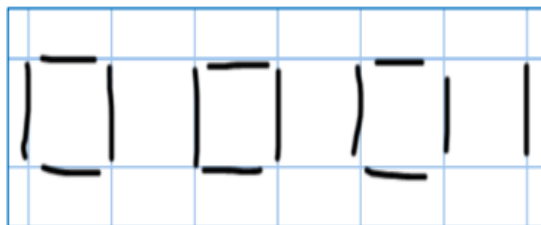
$$13 \div 4$$

Use of lollipop sticks to form wholes- squares are made because we are dividing by 4.



There are 3 whole squares, with 1 left over.

Children to represent the lollipop sticks pictorially.

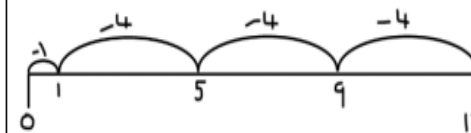


There are 3 whole squares, with 1 left over.

$$13 \div 4 = 3 \text{ remainder } 1$$

Children should be encouraged to use their times table facts; they could also represent repeated addition on a number line.

'3 groups of 4, with 1 left over'



**Sharing using place value counters.**

$$42 \div 3 = 14$$



10s	1s



10s	1s
●	
●	
●	



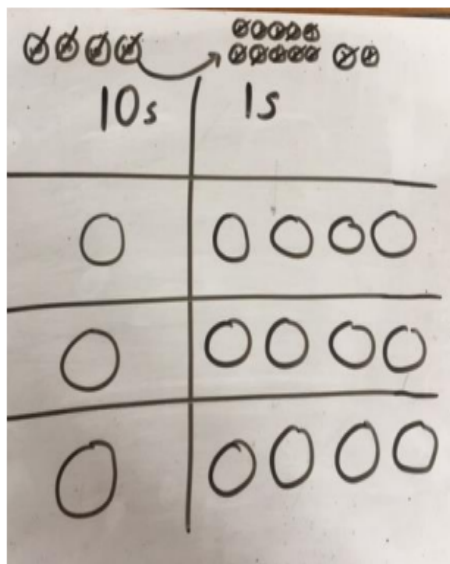
10s	1s
●	●●●●
●	●●●●
●	●●●●

= 14



10s	1s
●	
●	
●	

Children to represent the place value counters pictorially.



Children to be able to make sense of the place value counters and write calculations to show the process.

$$42 \div 3$$

$$42 = 30 + 12$$

$$30 \div 3 = 10$$

$$12 \div 3 = 4$$

$$10 + 4 = 14$$

